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## Local Diffusion in Paramagnetic Solutions by NMR Relaxometry at One Frequency

Andrea Melchior and Pascal H. Fries\*

Laboratoire de Reconnaissance Ionique, Service de Chimie Inorganique et Biologique (UMR-E 3 CEA-UJF), CEA/DSM/Département de Recherche Fondamentale sur la Matière Condensée, CEA-Grenoble, F-38054 Grenoble Cédex 9, France

Received February 21, 2006; E-mail: fries@drfmc.ceng.cea.fr

Experimental studies of the unrestricted translational (t) diffusion coefficient  $D^t$  of molecules in a liquid provide information<sup>1</sup> about the organization of their immediate environment and a way to test the models of intermolecular forces and the theories of transport. In porous media and biological tissues,  $D^t$  is important to correlate the long-range apparent diffusion<sup>2</sup> of the molecules explored by pulsed gradient spin—echo (PGSE) NMR with their interactions with the fluid/matrix interfaces and/or macromolecules in a crowded environment. Here, a simple method is proposed to measure the relative diffusion coefficient of a pair of small molecules at the nanometer scale. It is easy to use on standard spectrometers and magnetic resonance (MR) imaging (I) and microscopy (M) instruments.

In a liquid solution, consider nuclear spins *I* on solvent or solute molecules  $M_I$  in the presence of electronic spins *S* on solutes  $M_S$ without long-ranged charge—charge or binding interaction with  $M_I$ . The longitudinal relaxation rate,  $R_1$ , transverse relaxation rate,  $R_2$ , and longitudinal relaxation rate,  $R_{1\rho}$ , in the rotating frame of a spin *I* can be measured in an external magnetic field **B**<sub>0</sub> by standard NMR sequences.<sup>3</sup> Each rate  $R_{\alpha}$  is the sum<sup>4</sup>  $R_{\alpha} = R_{\alpha 0} + R_{\alpha p}$  of the value  $R_{\alpha 0}$  in the diamagnetic solution without paramagnetic solutes and of the paramagnetic (p) relaxation enhancement (PRE)  $R_{\alpha p}$  of the spin *I* due to its purely outer-sphere (OS) interactions with the spins *S*. The PREs  $R_{2p}$  and  $R_{1\rho p}$  are indistinguishable, but are in extremely viscous solvents.<sup>4</sup> The mixed PRE is defined as<sup>4</sup>

$$R_{\rm mix} = R_{\rm mix2} \equiv \frac{3}{2} \left( R_{\rm 2p} - \frac{R_{\rm 1p}}{2} \right) \simeq R_{\rm mix1\rho} \equiv \frac{3}{2} \left( R_{\rm 1\rho p} - \frac{R_{\rm 1p}}{2} \right)$$
(1)

The relaxivity,  $r_{\alpha}$  [s<sup>-1</sup> mM<sup>-1</sup>] ( $\alpha$  = 1, 2, 1 $\rho$ , mix), is defined as the PRE  $R_{\alpha\rho}$  divided by the concentration  $c_S$  [mM] of  $M_S$ 

$$r_{\alpha} \equiv R_{\alpha p}/c_{S} = (R_{\alpha} - R_{\alpha 0})/c_{S}$$
(2)

The relative diffusion coefficient *D* of  $M_I$  and  $M_S$  can be derived from three properties, *P*1, *P*2, and *P*3, of  $r_{mix}$  and  $r_1$ . The method was tested in the case of the proton PREs of the *tert*-butyl alcohol  $M_I = (CH_3)_3COD$  due to the paramagnetic complex  $M_S =$  $Gd(dtpa)^{2-}$  in a D<sub>2</sub>O solution with  $(dtpa)^{5-} =$  diethylenetriamine pentaacetate. Let  $\gamma_I$  and  $\gamma_S$  be the gyromagnetic ratios of the spins *I* and *S*, and  $\omega_I \equiv |\gamma_I|B_0$  and  $\omega_S \equiv |\gamma_S|B_0$ , their angular Larmor frequencies. The relaxation theory used to derive *D* involves the OS variation parameter  $\lambda_D \equiv (8\pi/45)\gamma^2_I\gamma^2_S\hbar^2 S(S+I)10^{-6}N_{Avogadro}$ . To discuss P1-P3, auxiliary geometrical and dynamical molecular quantities are introduced: denote the collision diameter of  $M_I$  and  $M_S$  by *b* and their translational correlation time by  $\tau \equiv b^2/D$ . It is assumed that the longitudinal electronic time correlation function<sup>4,5</sup> (TCF)  $G_{II}^{nor}(t) \equiv \langle S_z(t)S_z(0) \rangle/\langle S_z(0) S_z(0) \rangle$  of the spin *S* is a decaying exponential with an electronic relaxation time  $T_{1e}$ . This assumption



*Figure 1.* Relaxivities  $r_{\alpha}$  ( $\alpha = 1$ , mix2, mix1 $\rho$ ) versus ( $\nu_l$ )<sup>1/2</sup> in D<sub>2</sub>O at 298 K.

holds for nitroxide radicals and complexed paramagnetic metal ions in *S* states (L = 0), such as Mn<sup>2+</sup> or Gd<sup>3+</sup> at sufficiently high field values.<sup>5</sup>

(P1) Above a moderate field  $B_0 \ge B_0^{\text{indep}} (B_0^{\text{indep}} \ge 1.5 \text{ T for } \text{Gd}(\text{III}) \text{ spins}), r_{\text{mix}}(B_0)$  reaches the infinite-field value  $r_{\text{mix}}(\infty)$ 

$$r_{\rm mix}(B_0) \cong r_{\rm mix}(\infty) \equiv r_{\rm mix}(B_0 = \infty) \tag{3}$$

so that it becomes independent of field.

The measured proton relaxivity,  $r_{\text{mix}}$ , of  $M_I$  versus  $v_I^{1/2}$  [MHz<sup>1/2</sup>] is reported in Figure 1. In the frequency interval, 0–20 MHz, it grows markedly because the electronic relaxation time  $T_{1e}$  increases rapidly<sup>5</sup> and becomes significantly longer than  $\tau$ . Then, the increase of  $T_{1e}$  has less effect. At a field  $B_0^{\text{indep}} \ge 3-4$  T (120 MHz),  $r_{\text{mix}}$  reaches a plateau, where  $r_{\text{mix}} = r_{\text{mix}}(\infty) = 4.1 \text{ s}^{-1} \text{ mM}^{-1}$  to within the experimental accuracy of 2–3%.

(P2) In the OS medium-field range defined by<sup>4</sup>  $\omega_l \tau < 1$  and  $\omega_s \tau \gg 1$ , for  $B_0 \ge B_0^{\text{indep}}$ , the longitudinal relaxivity is

$$r_1 \simeq r_{\text{mix}} - (\lambda_D / D^{3/2}) \sqrt{\pi \nu_I} \simeq r_{\text{mix}}(\infty) - (\lambda_D / D^{3/2}) \sqrt{\pi \nu_I} \quad (4)$$

If  $B_0 \ge B_0^{\text{indep}}$ , the inequality  $(r_{\text{mix}} - r_1) \le 0.5r_{\text{mix}}$  is a conservative rule ensuring that eq 4 holds.

The experimental  $r_1$  versus  $v_I^{1/2}$  [MHz<sup>1/2</sup>] is shown in Figure 1. The frequency axis can be split into three field ranges: in the "low"-field range below 120 MHz,  $r_1$  depends on the details<sup>4-6</sup> of the relative translational and rotational motions of the interacting species and on the electronic relaxation. Its behavior, just as that of  $r_{\text{mix}}$ , has no simple features. In the OS medium-field (mf) range from  $v_{Imin}^{\text{mf}} = 120$  MHz to  $v_{Imax}^{\text{mf}} = 800$  MHz,  $r_1$  shows the linear decrease in  $v_I^{1/2}$  of eq 4. The relative diffusion coefficient  $D = 0.88 \times 10^{-5}$  cm<sup>2</sup> s<sup>-1</sup> is readily obtained from the  $r_1$  and  $r_{\text{mix}}(\infty)$  values measured at one frequency. In the "high"-field range  $v_I \ge v_{Imax}^{\text{mf}}$ ,  $r_1$  is again a complicated function depending on the details of the interacting species.



Figure 2. Relative diffusion coefficients versus  $T/\eta$  in D<sub>2</sub>O.

(P3) For 
$$B_0 \ge B_0^{\text{indep}}$$
, D is inversely proportional to  $r_{\text{mix}}$ 

$$D = k_{\rm solv} / r_{\rm mix} = D^{\rm ref} r_{\rm mix}^{\rm ref} / r_{\rm mix}$$
(5)

where  $k_{solv}$  is determined by the solvent, that is, the more numerous species. The solvent-related parameter  $k_{solv}$  depends very little on the temperature, pressure, and concentrations of reasonable amounts of added neutral or charged spectator species in the solution.<sup>7</sup> Here, spectator species are defined as molecules which do not bind to  $M_I$  or  $M_S$  for durations of the order of  $\tau$  or longer. An experimental estimate of  $k_{\text{solv}}$  is  $k_{\text{solv}} = D^{\text{ref}} r_{\text{mix}}^{\text{ref}}$ , where  $D^{\text{ref}}$  and  $r_{\text{mix}}^{\text{ref}}$  are the measured values for the  $M_I/M_S$  pair in a chosen reference (ref) system.

The reference system is the  $(CH_3)_3COD/Gd(dtpa)^{2-}$  pair in D<sub>2</sub>O at 298 K. The coefficient D, obtained between 283 and 343 K from eq 5, is plotted versus  $T/\eta$  in Figure 2, where it compares very well with its usual definition as the sum

$$D^{\rm sum} = D_I^{\rm t} + D_S^{\rm t} \tag{6}$$

of the self-diffusion coefficients  $D_I^t$  and  $D_S^t$  of  $(CH_3)_3COD$  and  $Lu(dtpa)^{2-}$ , representing Gd(dtpa)^{2-}, which were measured by the PGSE NMR technique.<sup>4,8</sup>

The applicability of eq 5 was further tested by adding fair amounts of viscous glycerol or KCl in the reference solution. In the glycerol- $d_8/D_2O$  mixture containing 42% w/w of glycerol, the viscosity increase by a factor of  $\sim$ 3.4 implies a similar reduction of the diffusion rates  $D = 0.247 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$  from eq 5 and  $D^{\text{sum}} = 0.243 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$ , which are in good agreement. When adding 2.65 M of KCl,  $D = 0.835 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$  from eq 5 and  $D^{\text{sum}} = 0.854 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$  change very little with respect to the reference values because the viscosity of a water solution of KCl is not altered by a rather large concentration of this salt, and the self-diffusion of Gd(dtpa)<sup>2-</sup> is weakly reduced by the Coulomb interactions with the surrounding ions.1c

Moreover, if P1-P3 hold,  $c_s$  and D can be simultaneously estimated as  $c_S = x^3/y^2$  and  $D = x^2/y^2$  with  $x \equiv R_{\text{mix}}/k_{\text{solv}}$ ,  $y \equiv (R_{\text{mix}})$  $(-R_{1p})/(\lambda_D \pi^{1/2} \nu_I^{1/2})$  (see Tables S6, S10, S14).

It was recognized<sup>9</sup> early that PRE studies could provide information about local diffusion at the cost of an accurate and complex treatment involving several parameters. Here, P1-P3 allow one to extract relative diffusion rates from experiment with straightforward algebra. The practical implementation of the method for a given  $M_l/M_s$  pair is as follows. Take a field  $B_0$  (typically  $B_0 \ge 2$ T), where  $r_{\text{mix}}$  is independent of electronic relaxation. Determine the relative diffusion coefficient  $D^{ref}$  of  $M_I$  and  $M_S$  in a reference solution, for instance, by using P2. Measure  $r_{mix}^{ref}$  in this reference system. Measure  $r_{\text{mix}}$  in other solutions of  $M_I/M_S$  in the same solvent and apply P3 to derive D. If  $M_S$  is large enough for  $D_S^t$  to verify  $D_S^t$  $\ll D_I^{t}$ , the method can serve to obtain the self-diffusion coefficient  $D_I^{\rm t} \simeq D$  of  $M_I$ . As noted previously,<sup>4</sup> since the molecular spatial dynamics responsible for the relaxivities takes place over distances of the order of a few nanometers, the method applies to molecular motions in confined media.<sup>2,10</sup> Its extension can be envisaged to large molecules,<sup>11</sup> in particular, if the PRE is induced by superparamagnetic particles,<sup>6d</sup> for which P1 and P3 hold.

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Supporting Information Available: Proofs of P1-P3, the raw experimental data, and complementary information are given in pp S1-S23. This material is available free of charge via the Internet at http:// pubs.acs.org.

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